



www.localsolver.com

Thierry Benoist Julien Darlay Bertrand Estellon
Frédéric Gardi Romain Megel Karim Nouioua

LocalSolver

Math programming by local search



LocalSolver

A solver aligned with enterprise needs

- Provides high-quality solutions in seconds
- Scalable: to tackle problems with millions of decisions
- Proves optimality when possible (best effort)

A solver aligned with practitioner needs

- « Model & Run »
 - Simple mathematical modeling formalism
 - Direct resolution: no need of complex tuning
- A simple and transparent pricing



A new-generation solver

- **Computing good-quality solutions by local search**
- Computing lower bounds separately (relaxation, inference, cuts)

A quality software

- An innovative modeling language for fast prototyping
- Lightweight object-oriented APIs: a few classes only
- Reliable and robust: quality assurance through continuous integration
- Fully portable: Windows, Linux, Mac OS (x86, x64)
- Reactive support, realized by developers themselves (even for academics)



Why local search?

Weaknesses of tree search

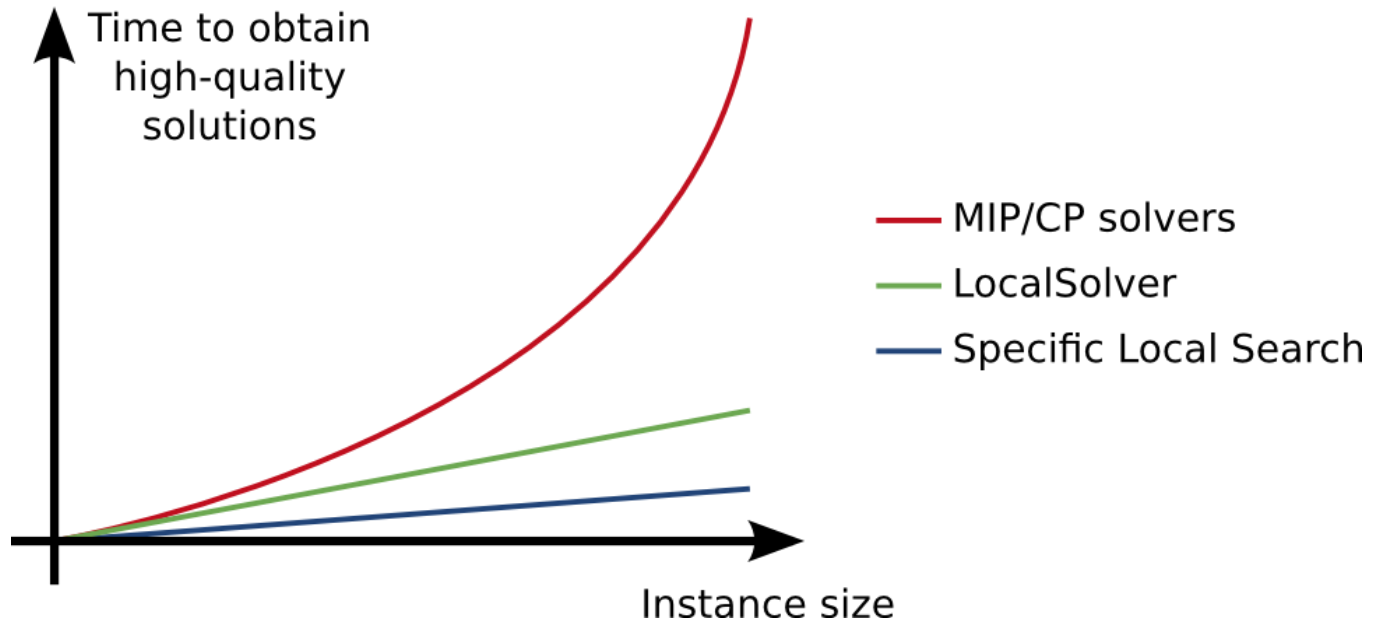
- Not suited to reach quickly good “integer feasible solutions”
- Designed to prove optimality
- Exponential time: not scalable (the best MIP solvers still fail to find feasible solutions for real-life instances with 10,000 binaries)

Benefits of local search

- Provides good-quality solutions in short running times
- Scalable (each iteration done in sublinear or even constant time)
- Able to optimize in nonconvex and nonsmooth spaces



Why local search?



LocalSolver

Quick tour



Knapsack

8 items to pack in a sack: maximize the total value of items while not exceeding a total weight of 102 kg

```
function model() {  
  // 0-1 decisions  
  x_0 <- bool(); x_1 <- bool(); x_2 <- bool(); x_3 <- bool();  
  x_4 <- bool(); x_5 <- bool(); x_6 <- bool(); x_7 <- bool();  
  
  // weight constraint  
  knapsackWeight <- 10*x_0+ 60*x_1+ 30*x_2+ 40*x_3+ 30*x_4+ 20*x_5+ 20*x_6+ 2*x_7;  
  constraint knapsackWeight <= 102;  
  
  // maximize value  
  knapsackValue <- 1*x_0+ 10*x_1+ 15*x_2+ 40*x_3+ 60*x_4+ 90*x_5+ 100*x_6+ 15*x_7;  
  maximize knapsackValue;  
}
```

Binary decision variables

Integer intermediate variables

The user writes the model: nothing else to do!
declarative approach = model & run



Multiobjective knapsack

```
function model() {  
  // 0-1 decisions  
  x[0..7] <- bool();  
  
  // weight constraint  
  knapsackWeight <- 10*x[0]+ 60*x[1]+ 30*x[2]+ 40*x[3]+ 30*x[4]+ 20*x[5]+ 20*x[6]+ 2*x[7];  
  constraint knapsackWeight <= 102;  
  
  // maximize value  
  knapsackValue <- 1*x[0]+ 10*x[1]+ 15*x[2]+ 40*x[3]+ 60*x[4]+ 90*x[5]+ 100*x[6]+ 15*x[7];  
  maximize knapsackValue;  
  
  // secondary objective: minimize product of minimum and maximum values  
  knapsackMinValue <- min[i in 0..7](x[i] ? values[i] : 1000);  
  knapsackMaxValue <- max[i in 0..7](x[i] ? values[i] : 0);  
  knapsackProduct <- knapsackMinValue * knapsackMaxValue;  
  minimize knapsackProduct;  
}
```

Nonlinear operators: prod, min, max,
and, or, if-then-else, ...

Lexicographic objectives



Mathematical operators

Arithmetic		Logical	Relational
sum	prod	not	==
min	max	and	!=
div	mod	or	<=
abs	dist	xor	>=
sqrt	log	if	<
			>



Modeling language

```
function model() {
```

```
    // 0-1 decisions
```

```
    x[1..nk
```

```
    // wei
```

```
    knapsa
```

```
    constr
```

```
    // max
```

```
    knapsa
```

```
    maxim
```

```
}
```

```
#include "localsolver.h"
```

```
using namespace localsolver.*;
```

```
int main()
```

```
{
```

```
    int weight
```

```
    int value
```

```
    LocalSolve
```

```
    LSModel*
```

```
    // 0-1 de
```

```
    LSExpress
```

```
    for (int
```

```
        x[i] =
```

```
    // knapsa
```

```
    LSExpress
```

```
    for (int
```

```
        knapsac
```

```
    // knapsa
```

```
    LSExpress
```

```
    for (int
```

```
        knapsac
```

```
    // knapsa
```

```
    model->ad
```

```
    // knapsa
```

```
    LSExpress
```

```
    for (int
```

```
        knapsac
```

```
    // maxim
```

```
    model->ad
```

```
    // close
```

```
    model->cl
```

```
    LSPhase*
```

```
    phase->se
```

```
    localsolv
```

```
    return 0;
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
import localsolver.*;
```

```
public class
```

```
{
```

```
    public stati
```

```
        int[] weig
```

```
        int[] val
```

```
    public class Toy
```

```
    {
```

```
        static void Main()
```

```
        {
```

```
            int[] weights = {10, 60, 30, 40, 30, 20, 20, 2};
```

```
            int[] values = {1, 10, 15, 40, 60, 90, 100, 15};
```

```
            LocalSolver localsolver = new LocalSolver();
```

```
            LSModel model = localsolver.GetModel();
```

```
            // 0-1 decisions
```

```
            LSExpression[] x = new LSExpression[8];
```

```
            for (int i = 0; i < 8; i++)
```

```
                x[i] = model.CreateExpression(LSOperator.Bool);
```

```
            // knapsackWeight <- 10*x0 + 60*x1 + 30*x2 + 40*x3 + 30*x4 + 20*x5 + 20*x6 + 2*x7;
```

```
            LSExpression knapsackWeight = model.CreateExpression(LSOperator.Sum);
```

```
            for (int i = 0; i < 8; i++)
```

```
                knapsackWeight.AddOperand(model.CreateExpression(LSOperator.Prod, weights[i], x[i]));
```

```
            // knapsackWeight <= 102;
```

```
            model.AddConstraint(model.CreateExpression(LSOperator.Leq, knapsackWeight, 102));
```

```
            // knapsackValue <- 1*x0 + 10*x1 + 15*x2 + 40*x3 + 60*x4 + 90*x5 + 100*x6 + 15*x7;
```

```
            LSExpression knapsackValue = model.CreateExpression(LSOperator.Sum);
```

```
            for (int i = 0; i < 8; i++)
```

```
                knapsackValue.AddOperand(model.CreateExpression(LSOperator.Prod, values[i], x[i]));
```

```
            // maximize knapsackValue;
```

```
            model.AddObjective(knapsackValue, LSObjectiveDirection.Maximize);
```

```
            // close the model before solving it
```

```
            model.Close();
```

```
            LSPhase phase = localsolver.CreatePhase();
```

```
            phase.SetTimeLimit(1);
```

```
            localsolver.Solve();
```

```
        }
```

```
    }
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

```
}
```

C++

Java

C#



LocalSolver

Real-life applications



Car sequencing

Scheduling cars along an assembly line

- Each car requires some options
- Each option induces a ratio constraint P/Q
- A class is a set of cars requiring the same options



Objective: to space options over the line

- We wish no more than 2 sunroofs over 5 consecutive cars
- For any window of 5 cars, a penalty is computed as $\max(n-2, 0)$ with n the number of cars requiring a sunroof



LSP model

$x_{cp} = 1 \Leftrightarrow$ car of class c is in position p

```
x[1..nbClasses][1..nbPositions] <- bool();  
  
for [c in 1..nbClasses]  
  constraint sum[p in 1..nbPositions](x[c][p]) == card[c];  
  
for [p in 1..nbPositions]  
  constraint sum[c in 1..nbClasses](x[c][p]) == 1;  
  
op[o in 1..nbOptions][p in 1..nbPositions] <- or[c in 1..nbClasses : options[c][o]](x[c][p]);  
  
nbVehicles[o in 1..nbOptions][j in 1..nbPositions-Q[o]+1] <- sum[k in 1..Q[o]](op[o][j+k-1]);  
  
violations[o in 1..nbOptions][j in 1..nbPositions-Q[o]+1] <- max(nbVehicles[o][j] - P[o], 0);  
  
obj <- sum[o in 1..nbOptions][p in 1..nbPositions-Q[o]+1](violations[o][p]);  
minimize obj;
```



Car sequencing at Renault

Additional constraints: no more than 10 consecutive cars with the same color



```
color[p in 1..nbPositions] <- sum[c in 1..nbClasses](color[c] * x[c][p]);  
same[p in 2..nbPositions] <- color[p] == color[p-1];  
toolong[p in 11..nbPositions] <- and[j in p-10..p](same[j]);  
for [p in 11..nbPositions] constraint not(toolong[p]);
```

Decision variables
remain the same

Additional objective: minimize the number of paint color changes

```
minimize sum[i in 2..nbPositions](not(same[i]));
```

Problem posed by Renault as 2005 ROADEF Challenge
LocalSolver competitive with finalists (ranked 16/55)



2012 ROADEF Challenge

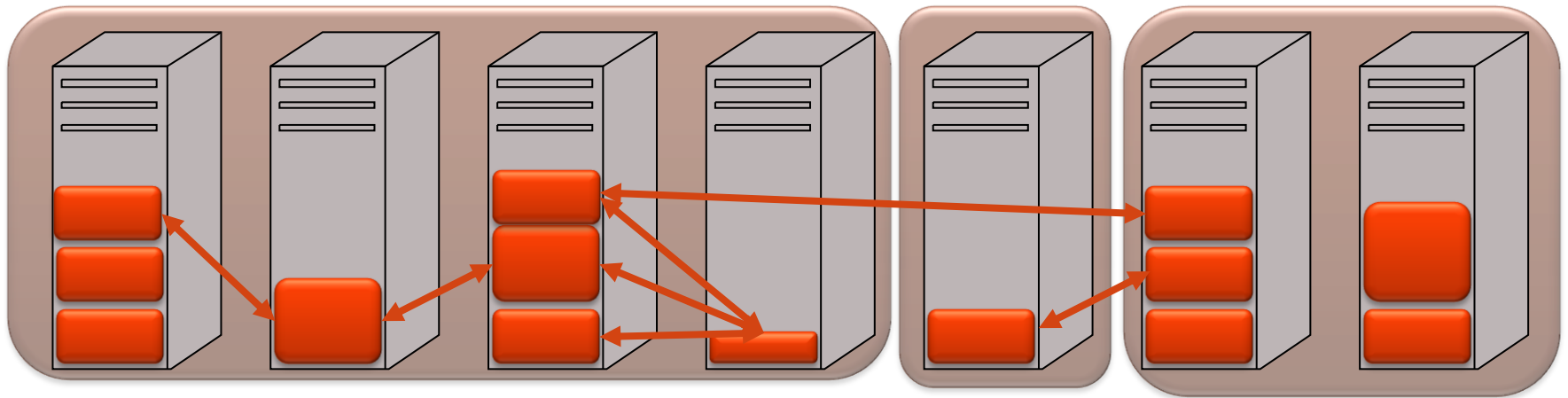


EURO



Google™

Reassignment of processes to machines, with different kinds of constraints (mutual exclusion, resources, etc.)



More than 100 000 binary decisions

Only 1 day of work

LocalSolver qualified for final round (ranked 25/80)

Our clients and users



LocalSolver

For more details



T. Benoist, B. Estellon, F. Gardi, R. Megel, K. Nouioua.
LocalSolver 1.x: a black-box local-search solver for 0-1 programming.
4OR, A Quarterly Journal of Operations Research 9(3), pp. 299-316.

<http://www.localsolver.com>

